

Reactor Design Python Code

April 1, 2019

```
In [2]: import numpy as np
import matplotlib.pyplot as plt
from scipy.integrate import odeint

In [60]: #Initial Conditions
Fao=2.5
Fbo=0
Fco=0
inivalues=[Fao,Fbo,Fco]

#Parameters
k = 0.0442784555801
T=400
Pao =10
R = 0.08206
c_To=Pao/(0.08206*T) #total concentration

def pfr(z,V):
    [Fa,Fb,Fc]=z #assignment of dependent variables to convenient variable names

    #Stoichiometry

    Ft=(Fa+Fb+Fc) #Total molar flowrate
    Ca=c_To*(Fa/Ft)
    Cb=c_To*(Fb/Ft)
    Cc=c_To*(Fc/Ft)

    #Rate
    ra = -k*Ca
    rb = -ra
    rc = -2*ra

    #MB
    dFadV = ra
    dFbdV = rb
    dFcdV = rc
```

```

    return dFadV, dFbdV, dFcdV

Vspan = np.linspace(0,1200,1500) # independent variable array: 200 pts from V=0 to V=
solver = odeint(pfr,inivalues,Vspan) # solver output has format [X,y]

# Plot results
plt.plot(Vspan,solver[:,0], label='F_A')
plt.plot(Vspan,solver[:,1], label='F_B')
plt.plot(Vspan,solver[:,2], label='F_C')

plt.xlabel('V (L)')
plt.ylabel('X and Flowrates (mol/Min)')

plt.title('Problem 3')

X_target=solver[:,0]
X=[]
for i in range(1500):
    X.append((2.5-X_target[i])/2.5) # (initial-final)/initial
plt.plot(Vspan, X, label='X')
plt.grid(True)
plt.legend(loc = 'best')
plt.show()

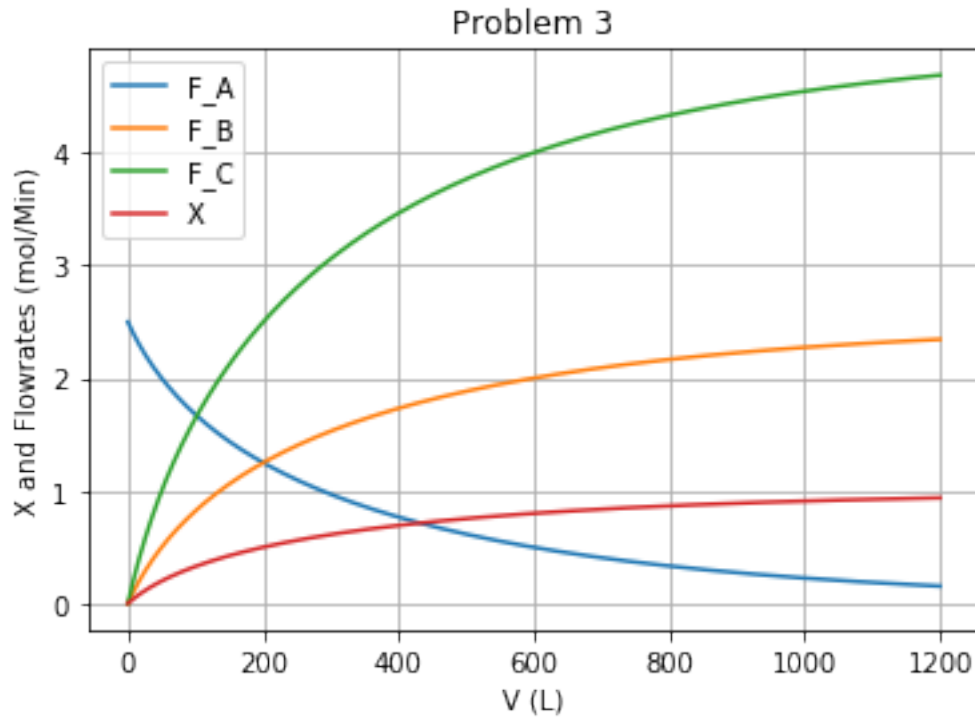
Vol=np.interp(0.9,X,Vspan)
index=int(Vol) # integer form of the Volume at which 90% conversion happens

A=np.array(solver[:,0])
B=np.array(solver[:,1])
C=np.array(solver[:,2])
print (A[index])#Flowrate of A at 90% conv.
print (B[index])#flowrate of A at 90% conv.
print (C[index])#flowrate of A at 90% conv.

Ftotal=A[index]+B[index]+C[index]
SpaceTime= Vol/Ftotal

print("Volume needed for 90% conversion is {:.2f} L. SpaceTime needed for 90% convers:

```



0.362065645038

2.13793435496

4.27586870992

Volume needed for 90% conversion is 946.61 L. SpaceTime needed for 90% conversion is 139.70 min

In [77]: #4a

```

#Initial conditions
Fao=2.5 #[mol/min]
Fbo=0
Fco=0
inivalues=[Fao,Fbo,Fco]
#Parameters
T=400
P_ao=10
R=0.08206
kc=0.08*60 #MTC
k = 0.0442784555801 #same as in Problem 3

def memreact(z,V):
    c_To=P_ao/(R*T) #total concentration
    Kc=0.025

```

```

[Fa,Fb,Fc]=z

#Stoichiometry
Ft=Fa+Fb+Fc
ca=c_To*Fa/Ft
cb=c_To*Fb/Ft
cc=c_To*Fc/Ft

#rate laws
ra = -k*(ca-cb*(cc**2)/Kc)
rb = -ra
rc = -2*ra

#MB
dFadV = ra
dFbdV = rb
dFcdV = rc

return dFadV, dFbdV, dFcdV

Vspan = np.linspace(0,1000,1500)
solver = odeint(memreact,inivalues,Vspan)
# Plot results
plt.plot(Vspan,solver[:,0], label='F_A')
plt.plot(Vspan,solver[:,1], label='F_B')
plt.plot(Vspan,solver[:,2], label='F_C')
plt.xlabel('V (L)')
plt.ylabel('Molar Flowrates (mol/min)')
plt.title('Problem 4(a and b)')

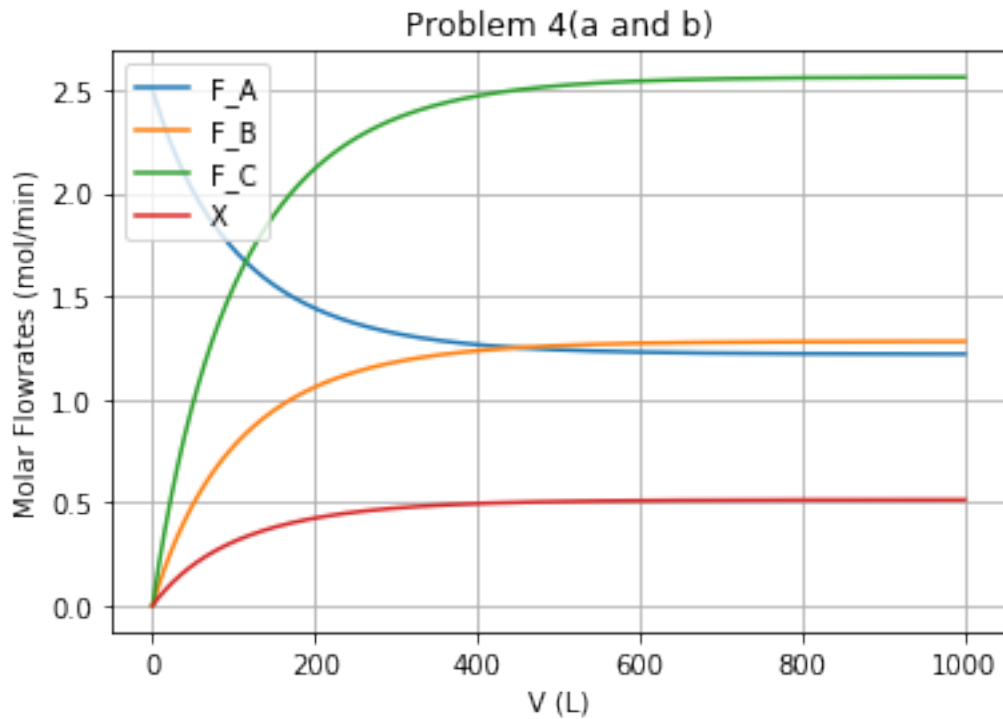
Xout=(Fao-solver[-1,0])/Fao #get's final value
print('Maximum Conversion (Xe) = {:.2f}'.format((Xout)))
X_target=solver[:,0]
X=[]
for i in range(1500):
    X.append((2.5-X_target[i])/2.5)
plt.plot(Vspan, X, label='X')
plt.grid(True)
plt.legend(loc = 'best')
plt.show()

#4b

conv90=np.interp(Xout*0.9,X,Vspan)
print('The volume needed for 90% of the maximum conversion is = {:.1f} L.'.format(conv90))

```

Maximum Conversion (Xe) = 0.51



The volume needed for 90% of the maximum conversion is = 268.4 L.

In [78]: #4c

```

#Initial conditions
Fao=2.5 #[mol/min]
Fbo=0
Fco=0
inivalues=[Fao,Fbo,Fco]
#Parameters
T=400
P_ao=10
R=0.08206
kc=0.08*60 #MTC
k = 0.0442784555801 #same as in Problem 3

def memreact(z,V):
    c_To=P_ao/(R*T) #total concentration
    Kc=0.025
    [Fa,Fb,Fc]=z

```

```

#Stoichiometry
Ft=Fa+Fb+Fc
ca=c_To*Fa/Ft
cb=c_To*Fb/Ft
cc=c_To*Fc/Ft

#rate laws
ra = -k*(ca-cb*(cc**2)/Kc)
rb = -ra
rc = -2*ra
#MB
dFadV = ra
dFbdV = rb - kc*cb
dFcdV = rc

return dFadV, dFbdV, dFcdV

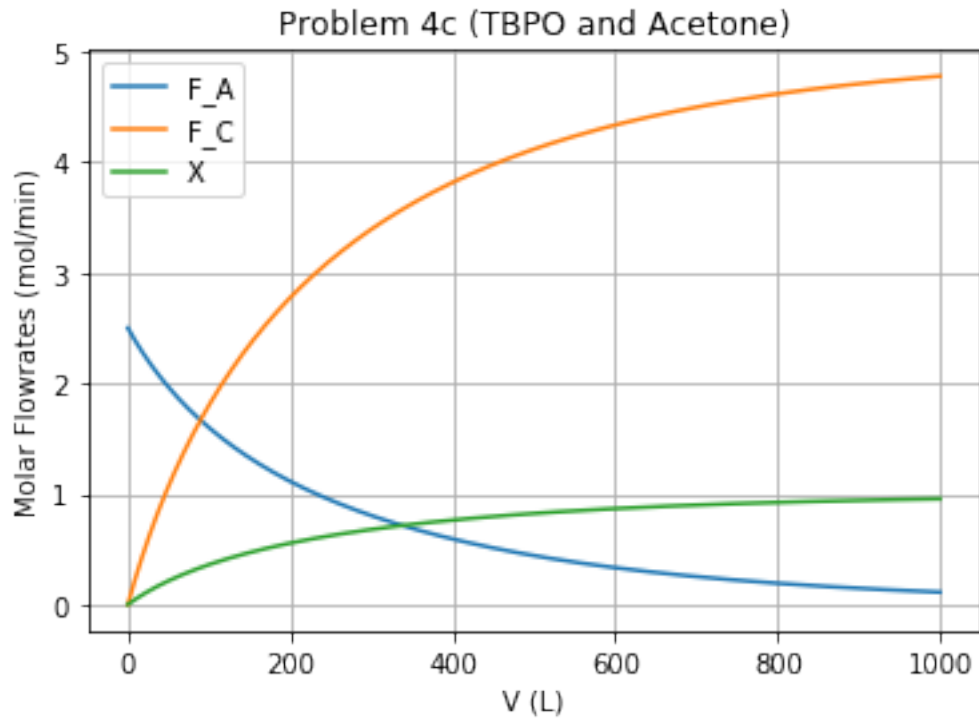
# Setup ODE solver
Vspan = np.linspace(0,1000,1500) # independent variable array: 200 pts from V=0 to V=
solver = odeint(memreact,inivalues,Vspan) # solver output has format [X,y]
#print(solver)

# Plot results
plt.plot(Vspan,solver[:,0], label='F_A')
plt.plot(Vspan,solver[:,2], label='F_C')
plt.xlabel('V (L)')
plt.ylabel('Molar Flowrates (mol/min)')
plt.title('Problem 4c (TBPO and Acetone)')

Xout=(Fao-solver[-1,0])/Fao #(initial-final)/initial
print('At reactor outlet, X_A ={: .2f}'.format((Xout)))
X_target=solver[:,0]
X=[]
for i in range(1500):
    X.append((2.5-X_target[i])/2.5)
plt.plot(Vspan, X, label='X')
plt.grid(True)
plt.legend(loc = 'best')
plt.show()
conv80= np.interp(0.8,X,Vspan)
print('The volume needed for reaching 90% of the maximum conversion is',conv80,'L')

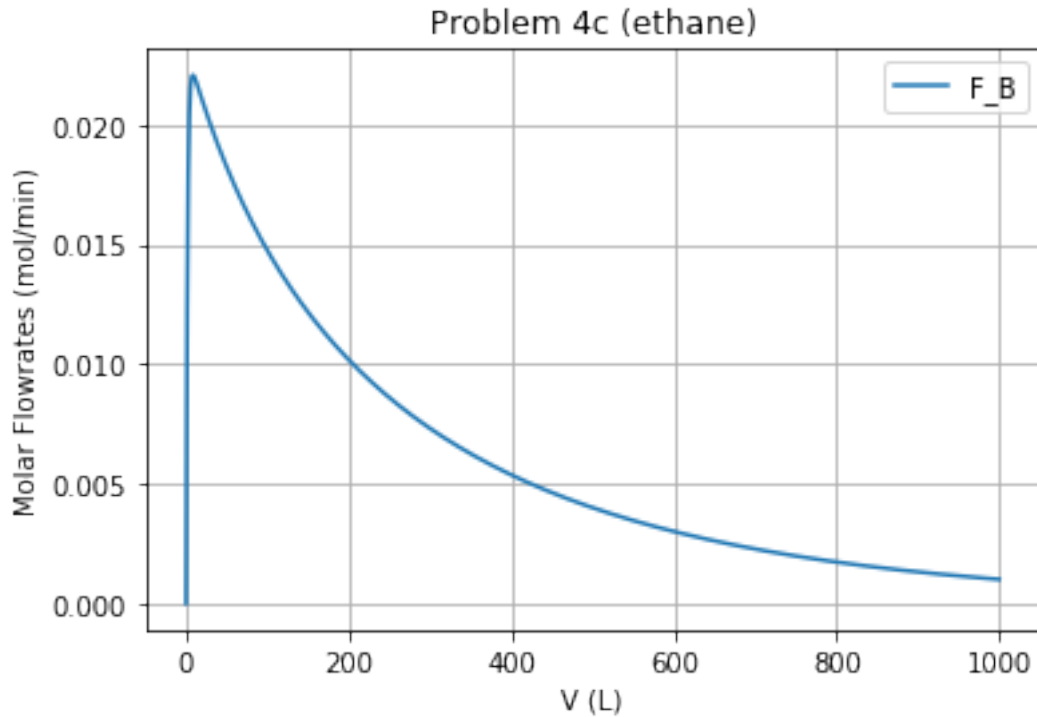
```

At reactor outlet, X_A =0.96



The volume needed for reaching 90% of the maximum conversion is 457.2671936581845 L

```
In [79]: plt.plot(Vspan,solver[:,1], label='F_B')
plt.xlabel('V (L)')
plt.ylabel('Molar Flowrates (mol/min)')
plt.legend(loc = 'best')
plt.title('Problem 4c (ethane)')
plt.grid(True)
plt.show()
```



```
In [24]: print('Maximum Flow rate of TBPO = {:.1f} mol/min.'.format(np.max(solver[:,0])))
         print('Maximum Flow rate of Ethane = {:.4f} mol/min.'.format(np.max(solver[:,1])))
         print('Maximum Flow rate of Acetone = {:.1f} mol/min.'.format(np.max(solver[:,2])))
```

```
Maximum Flow rate of TBPO = 2.5 mol/min.
Maximum Flow rate of Ethane = 0.0221 mol/min.
Maximum Flow rate of Acetone = 4.8 mol/min.
```

The maximum flow rate of TBPO (A) happens at the very beginning which is to be expected, as it will decrease as volume increases. The opposite is true for Acetone, having its maximum flow rate be at the very end of the 1000 L process, as its rate increases with volume. The oddity is with ethane, and that is because of the mass transfer coefficient. The permeability makes the ethane diffuse out of the reactor, so its flowrate decreases once the mass of the ethane is big enough to have its MTC play a large role, ie, after 0.0221 mol/min

```
In [3]: #2a
```

```
#Define all parameters
T = 680
Fao = 50
Pao = 10
R = 0.08206
Cao = Pao/(R*T)
```



```

Kbu=0.32
k = 0.054
alpha = 0.000
Wspan = [0,2000]
inivalues=[0,1.0]

# Set up the differential equations
def pbr(z,V):
    [X,y]=z

    ca = Cao*(1 - X)/(1 + X) #stoichiometry
    Pa=ca*R*T
    neg_ra = (k*Pa)/((1+Kbu*Pa)**2) #rate law

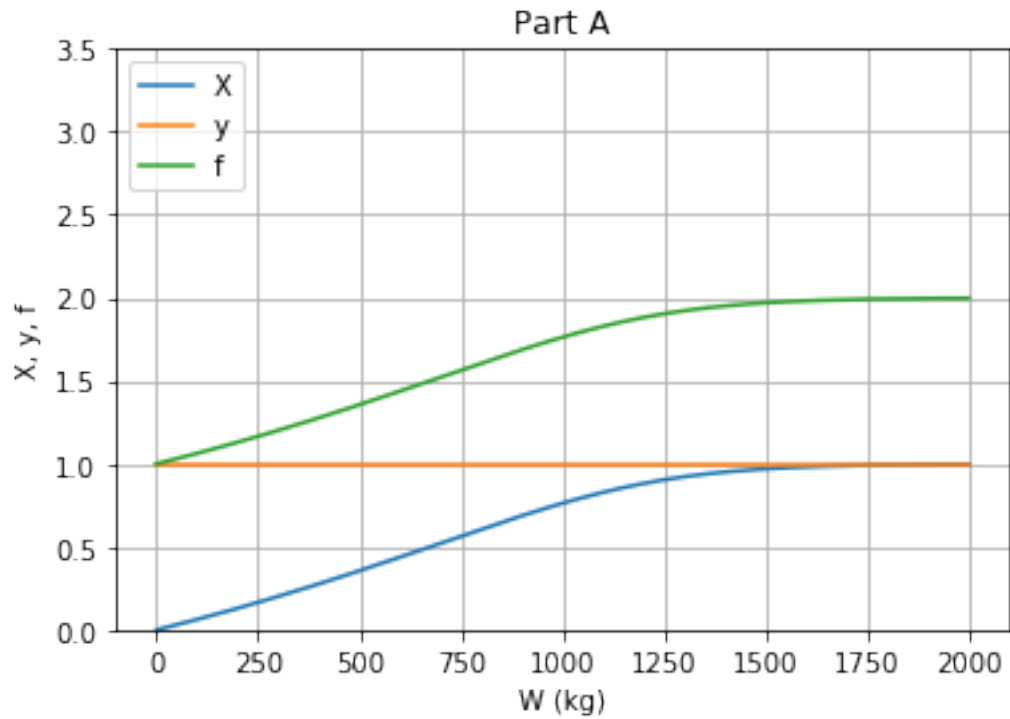
    #ODEs:
    dXdW = neg_ra/Fao
    dydW = -(alpha*(1+X))/(2*y) #Ergun equation
    return dXdW, dydW

# Setup ODE solver
V = np.linspace(Wspan[0],Wspan[1],200)
solver = odeint(pbr,inivalues,V)
X=solver[:,0]
y=solver[:,1]
f=(1+X)/y #Calculate f for each element in X and y vectors

# Plot results
plt.plot(V,X, label='X')
plt.plot(V,y, label='y')
plt.plot(V,f, label='f')
plt.xlabel('W (kg)')
plt.ylabel('X, y, f')
plt.title('Part A')
plt.legend(loc = 'upper left')
plt.grid(True)
plt.ylim(0,3.5)
plt.show()

#From X vs. W, find W required for 80% conversion
V_requirement=np.interp(0.8,X,V)
print('Reactor reaches a conversion of X = 80% at W =',str(V_requirement),'kg')

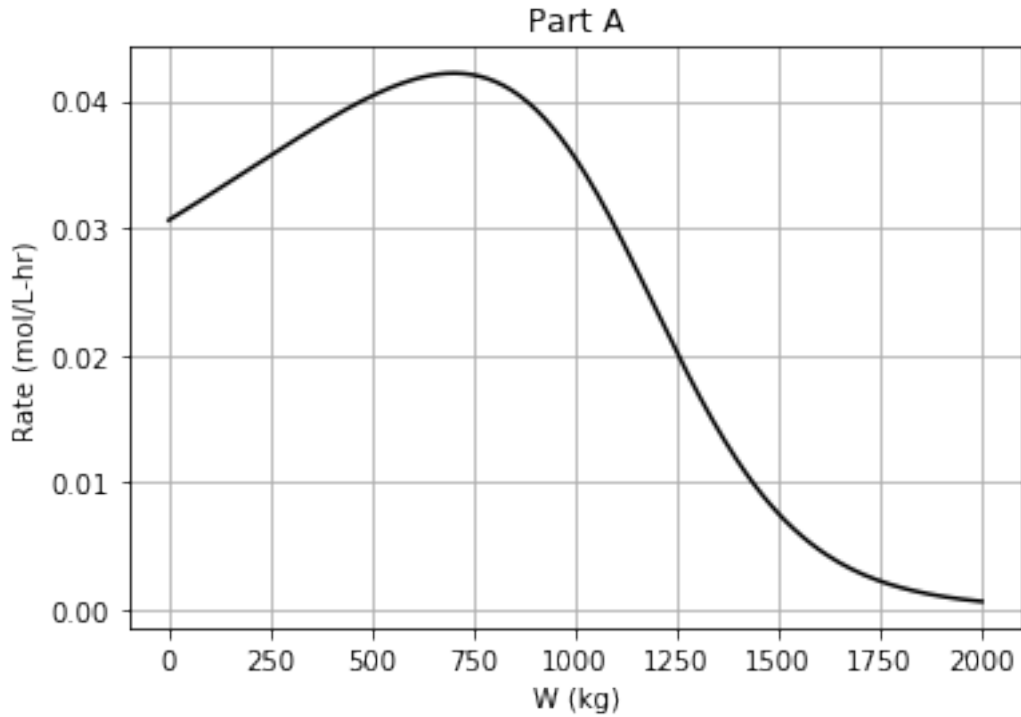
```



Reactor reaches a conversion of $X = 80\%$ at $W = 1054.1518509611706$ kg

```
In [4]: ca = Cao*(1 - X)/(1 + X) #stoichiometry
Pa=ca*R*T
neg_ra = (k*Pa)/((1+Kbu*Pa)**2) #rate law
```

```
plt.plot(V,neg_ra,'black')
plt.xlabel('W (kg)')
plt.title('Part A')
plt.ylabel('Rate (mol/L-hr)')
plt.grid(True)
plt.show()
```



In [5]: #2c

```

#Define all parameters
T = 680
Fao = 50
Pao = 10
R = 0.08206
Cao = Pao/(R*T)
KBu=0.32
k = 0.054
alpha = 0.0006
Vspan = [0,1000]
inivalues=[0,1.0]

# Set up the differential equations
def pbr2(z,V):
    [X,y]=z

    ca = (Cao*(1 - X)/(1 + X))*y #stoichiometry
    Pa=ca*R*T
    neg_ra = (k*Pa)/((1+KBu*Pa)**2) #rate law

    #ODEs:
    dXdV = neg_ra/Fao #mole balance

```

```

    dydV = -(alpha*(1+X))/(2*y) #Ergun equation
    return dXdV, dydV

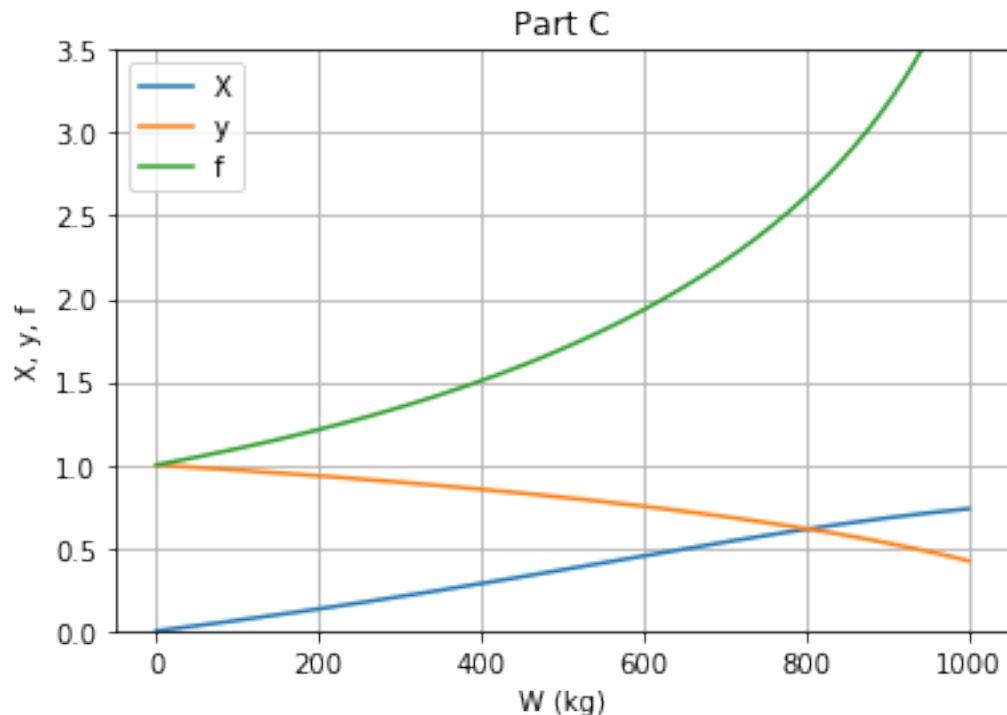
# Setup ODE solver
V = np.linspace(Vspan[0],Vspan[1],200) # independent variable array, increment 1
solver = odeint(pbr2,inivalues,V) # solver has format [X,y]

X=solver[:,0]
y=solver[:,1]
f=(1+X)/y #Calculate f for each element in X and y vectors

# Plot results
plt.plot(V,X, label='X')
plt.plot(V,y, label='y')
plt.plot(V,f, label='f')
plt.xlabel('W (kg)')
plt.ylabel('X, y, f')
plt.legend(loc = 'upper left')
plt.grid(True)
plt.title('Part C')
plt.ylim(0,3.5)
plt.show()

#From X vs. W, find W required for 70% conversion
V_requirement=np.interp(0.7,X,V)
print('Reactor reaches a conversion of X = 70% at W =',str(V_requirement),'kg')

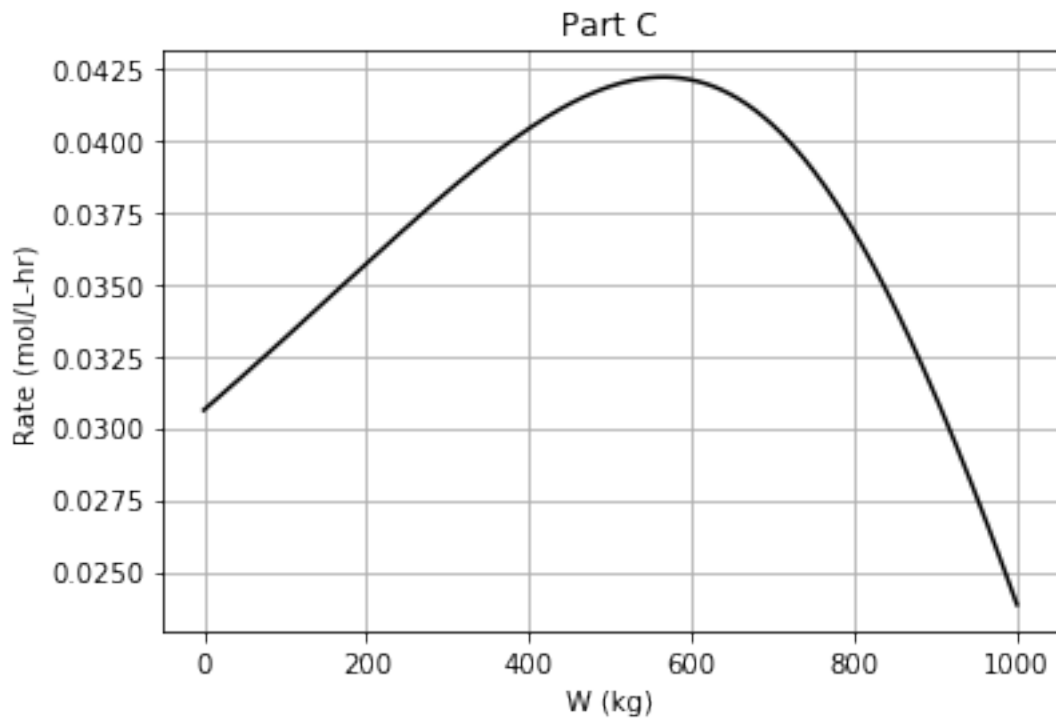
```



Reactor reaches a conversion of $X = 70\%$ at $W = 932.2674246272811$ kg

```
In [6]: ca = (Cao*(1 - X)/(1 + X))*y #stoichiometry
Pa=ca*R*T
neg_ra = (k*Pa)/((1+Kbu*Pa)**2) #rate law
```

```
plt.plot(V,neg_ra,'black')
plt.xlabel('W (kg)')
plt.ylabel('Rate (mol/L-hr)')
plt.title('Part C')
plt.grid(True)
plt.show()
```



```
In [7]: #Define all parameters
Cao=1
Cro=0
Cso=0
Cto=0
Cuo=0
```

```
k1=40
k2=10
k3=0.1
k4=.2
```

```
inivalues=[Cao,Cro,Cso,Cto,Cuo]
```

```
# Set up the differential equations
```

```
def pfr(z,t):
```

```
    [Ca,Cr,Cs,Ct,Cu]=z #assignment of dependent variables to convenient variable names
```

```
    r1a=-k1*Ca
```

```
    r1b=-k2*Ca
```

```
    r1r=-k3*Cr
```

```
    r2r=-k4*Cr
```

```
    ra=r1a+r1b
```

```
    rr=-r1a+r2r+r1r
```

```
    rt=-r1b
```

```
    rs=-r1r
```

```
    ru=-r2r
```

```
    dCadt=ra
```

```
    dCrdt=rr
```

```
    dCtdt=rt
```

```
    dCsdt=rs
```

```
    dCudt=ru
```

```
    return dCadt, dCrdt, dCsdt,dCtdt, dCudt
```

```
T = np.linspace(0,50,200) # independent variable array, increment 1
```

```
solver = odeint(pfr,inivalues,T) # solver has format [X,y]
```

```
CA=solver[:,0]
```

```
CR=solver[:,1]
```

```
CS=solver[:,2]
```

```
CT=solver[:,3]
```

```
CU=solver[:,4]
```

```
# Plot results
```

```

plt.plot(T, CA, label='CA')
plt.plot(T,CR, label='CR')
plt.plot(T,CS, label='CS')
plt.plot(T,CT, label='CT')
plt.plot(T,CU, label='CU')

plt.xlabel('time (sec)')
plt.ylabel('Concentration (M)')
plt.legend(loc = 'best')
plt.grid(True)
plt.show()

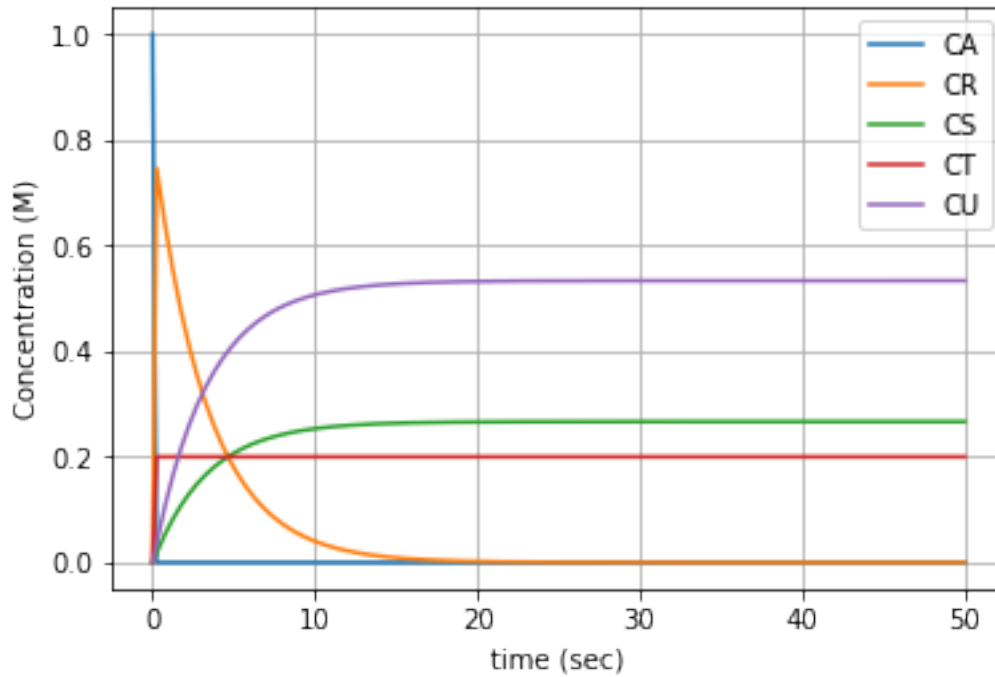
time=np.interp(0.2,CS,T)
print(time)
A_Final= np.interp(time,T,CA)
R_Final= np.interp(time,T,CR)
S_Final= np.interp(time,T,CS)
T_Final= np.interp(time,T,CT)
U_Final= np.interp(time,T,CU)

print("Final Concentration of A is {:.3f} M".format(A_Final))
print("Final Concentration of R is {:.3f} M".format(R_Final))
print("Final Concentration of S is {:.3f} M".format(S_Final))
print("Final Concentration of T is {:.3f} M".format(T_Final))
print("Final Concentration of U is {:.3f} M".format(U_Final))
#arg=np.argmax(CB)
#time=T[arg]
#vo=V/time

#print(MaxB)

#From X vs. W, find W required for 50% conversion
#V_requirement=np.interp(0.7,X,V)
#print('Reactor reaches a conversion of X = 70% at W =',str(V_requirement),'kg')

```



4.643402772774782

Final Concentration of A is -0.000 M

Final Concentration of R is 0.200 M

Final Concentration of S is 0.200 M

Final Concentration of T is 0.200 M

Final Concentration of U is 0.400 M

In [8]: *#Define all parameters*

Cao=1

Cro=0

Cso=0

Cto=0

Cuo=0

k1=0.02

k2=.01

k3=10

k4=20

inivalues=[Cao,Cro,Cso,Cto,Cuo]


```

# Set up the differential equations
def pfr(z,t):
    [Ca,Cr,Cs,Ct,Cu]=z #assignment of dependent variables to convenient variable names

    r1a=-k1*Ca
    r1b=-k2*Ca
    r1r=-k3*Cr
    r2r=-k4*Cr

    ra=r1a+r1b
    rr=-r1a+r2r+r1r
    rt=-r1b
    rs=-r1r
    ru=-r2r

    dCadt=ra
    dCrdt=rr
    dCtdt=rt
    dCsdt=rs
    dCudt=ru

    return dCadt, dCrdt, dCsdt,dCtdt, dCudt

T = np.linspace(0,300,200) # independent variable array, increment 1
solver = odeint(pfr,inivalues,T) # solver has format [X,y]

CA=solver[:,0]
CR=solver[:,1]
CS=solver[:,2]
CT=solver[:,3]
CU=solver[:,4]

# Plot results
plt.plot(T, CA, label='CA')
plt.plot(T,CR, label='CR')
plt.plot(T,CS, label='CS')
plt.plot(T,CT, label='CT')
plt.plot(T,CU, label='CU')

plt.xlabel('time (sec)')
plt.ylabel('Concentration (M)')
plt.legend(loc = 'best')

```

```

plt.grid(True)
plt.show()

time=np.interp(0.2,CS,T)
print(time)
A_Final= np.interp(time,T,CA)
R_Final= np.interp(time,T,CR)
S_Final= np.interp(time,T,CS)
T_Final= np.interp(time,T,CT)
U_Final= np.interp(time,T,CU)

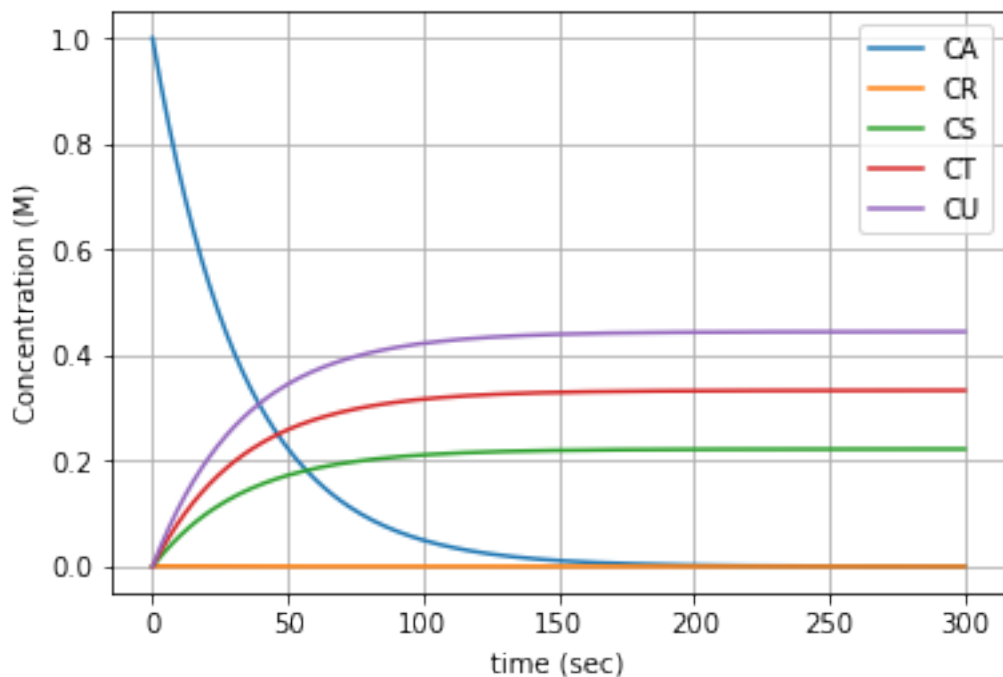
print("Final Concentration of A is {:.3f} M".format(A_Final))
print("Final Concentration of R is {:.3f} M".format(R_Final))
print("Final Concentration of S is {:.3f} M".format(S_Final))
print("Final Concentration of T is {:.3f} M".format(T_Final))
print("Final Concentration of U is {:.3f} M".format(U_Final))

#arg=np.argmax(CB)
#time=T[arg]
#vo=V/time

#print(MaxB)

#From X vs. W, find W required for 50% conversion
#V_requirement=np.interp(0.7,X,V)
#print('Reactor reaches a conversion of X = 70% at W =',str(V_requirement),'kg')

```



76.78827015068796

Final Concentration of A is 0.100 M

Final Concentration of R is 0.000 M

Final Concentration of S is 0.200 M

Final Concentration of T is 0.300 M

Final Concentration of U is 0.400 M

In [9]: *#Define all parameters*

Cao=0.018

Cbo=0.05

Cco=0

Cr1o=0

Cr2o=0

R=1.98588

T=80+273

k1=(4.87*10**6)*np.exp(-10080/(R*T))

k2=(3.49*10**3)*np.exp(-5965/(R*T))

L=6*12 *#in*

A=((1.25**2)/4)*np.pi

V=L*A *#in³*

V=V/61.0237#L

inivalues=[Cao,Cbo,Cco,Cr1o,Cr2o]

Set up the differential equations

def pfr(z,t):

[Ca,Cb,Cc,Cr1,Cr2]=z *#assignment of dependent variables to convenient variable nam*

r1a=-k1*Ca*Cb

r2b=-k2*Cr1*Cb

ra=r1a

rb=r1a+r2b

rc=-r1a-r2b

rR1=-r1a+r2b

rR2=-r2b

dCadt=ra

dCbdt=rb

```

dCcdt=rc
dcR1dt=rR1
dcR2dt=rR2

return dCadt, dCbdt, dCcdt, dcR1dt, dcR2dt

# Setup ODE solver
T = np.linspace(0,100,200) # independent variable array, increment 1
solver = odeint(pfr,inivalues,T) # solver has format [X,y]

CA=solver[:,0]
CB=solver[:,1]
CC=solver[:,2]
CR1=solver[:,3]
CR2=solver[:,4]

# Plot results
plt.plot(T, CA, label='CA')
plt.plot(T,CB, label='CB')
plt.plot(T,CC, label='CC')
plt.plot(T,CR1, label='CR1')
plt.plot(T,CR2, label='CR2 ')

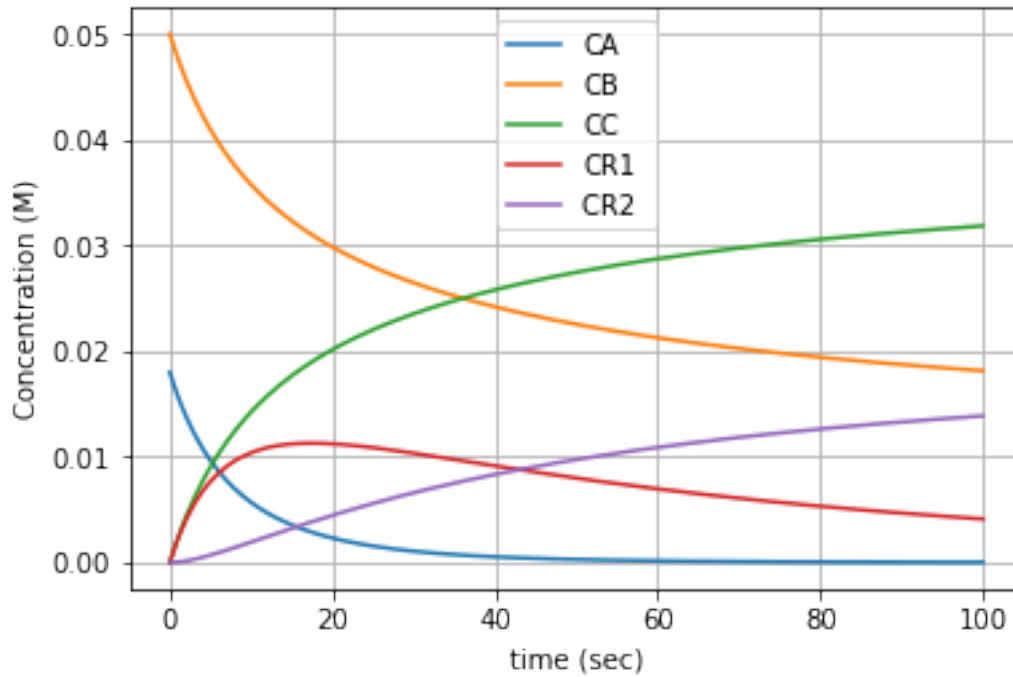
plt.xlabel('time (sec)')
plt.ylabel('Concentration (M)')
plt.legend(loc = 'best')
plt.grid(True)
plt.show()

MaxR1= np.max(CR1)
arg=np.argmax(CR1)
time=T[arg]
vo=V/time

print("A) The Flowrate that maximizes R1 is {:.4f} L/s".format(vo))
print("B) The Maximum effluent Concentration of R1 is {:.4f} mol/L".format(MaxR1))

#From X vs. W, find W required for 50% conversion
#V_requirement=np.interp(0.7,X,V)
#print('Reactor reaches a conversion of X = 70% at W =',str(V_requirement),'kg')

```



- A) The Flowrate that maximizes R1 is 0.0823 L/s
- B) The Maximum effluent Concentration of R1 is 0.0113 mol/L

```
In [10]: #Define all parameters
Cao=0.018
Cbo=0.05
Cco=0
Cr1o=0
Cr2o=0

R=1.98588
T=120+273
k1=(4.87*10**6)*np.exp(-10080/(R*T))
k2=(3.49*10**3)*np.exp(-5965/(R*T))

L=6*12 #in
A=((1.25**2)/4)*np.pi
V=L*A #in^3
V=V/61.0237#L

inivalues=[Cao,Cbo,Cco,Cr1o,Cr2o]
```

```

# Set up the differential equations
def pfr(z,t):
    [Ca,Cb,Cc,Cr1,Cr2]=z #assignment of dependent variables to convenient variable na

    r1a=-k1*Ca*Cb
    r2b=-k2*Cr1*Cb

    ra=r1a
    rb=r1a+r2b
    rc=-r1a-r2b
    rR1=-r1a+r2b
    rR2=-r2b

    dCadt=ra
    dCbdt=rb
    dCcdt=rc
    dcR1dt=rR1
    dcR2dt=rR2

    return dCadt, dCbdt, dCcdt, dcR1dt, dcR2dt

# Setup ODE solver
T = np.linspace(0,100,200) # independent variable array, increment 1
solver = odeint(pfr,inivalues,T) # solver has format [X,y]

CA=solver[:,0]
CB=solver[:,1]
CC=solver[:,2]
CR1=solver[:,3]
CR2=solver[:,4]

# Plot results
plt.plot(T, CA, label='CA')
plt.plot(T,CB, label='CB')
plt.plot(T,CC, label='CC')
plt.plot(T,CR1, label='CR1')
plt.plot(T,CR2, label='CR2 ')

plt.xlabel('time (sec)')
plt.ylabel('Concentration (M)')
plt.legend(loc = 'best')
plt.grid(True)
plt.show()

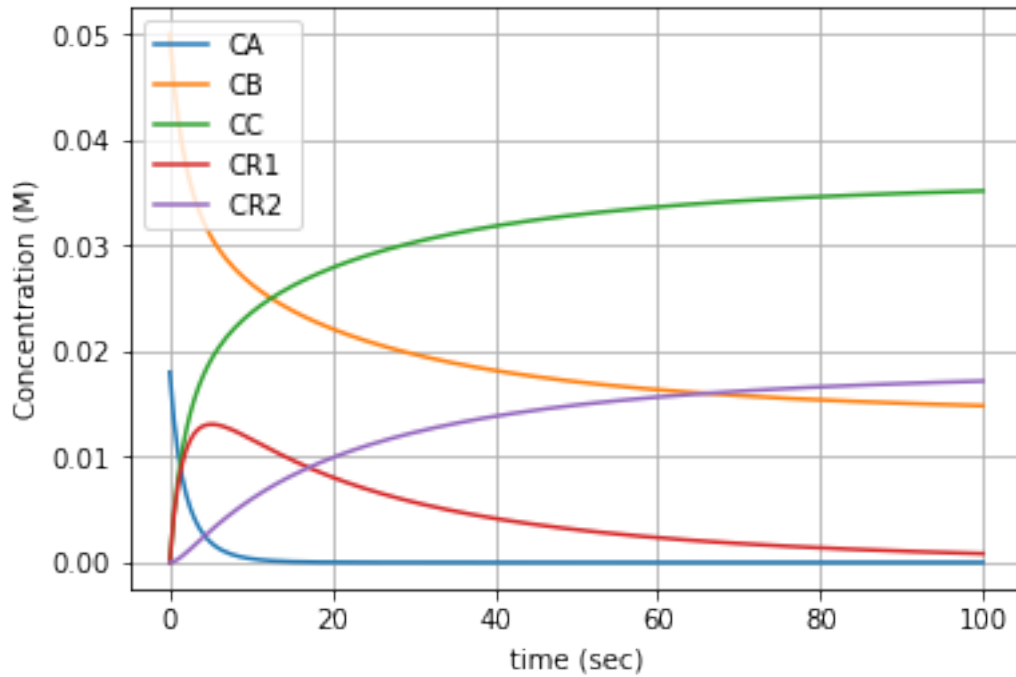
MaxR1= np.max(CR1)
arg=np.argmax(CR1)
time=T[arg]

```

```
vo=V/time
```

```
print("At 120 degrees Celsius,the Maximum effluent Concentration of R1 is {:.4f} M and
```

```
print("So increasing temperature will increase yield, but you will also need to increa
```



At 120 degrees Celsius,the Maximum effluent Concentration of R1 is 0.0131 M and the Flowrate t
So increasing temperature will increase yield, but you will also need to increase the flowrate

In []: